

Some quadratic equations in the form of  $ax^2 + bx + c = 0$  can be solved easily by factoring. For example, the equation  $x^2 + 6x - 16 = 0$  can be factored easily to  $(x + 8)(x - 2) = 0$  to give solutions of  $x = -8$  and  $x = 2$

When a quadratic equation cannot be factored using integers, you have two options. You can use the quadratic formula or you can use a method called **completing the square**. When  $a = 1$ , completing the square is the way to go (when  $a > 1$ , use the quadratic formula).

Example 1: Solve  $x^2 + 8x - 10 = 0$  by completing the square.

Since it cannot be factored using integers, Write the equation in the form $ax^2 + bx = -c$	$x^2 + 8x - 10 = 0$ $x^2 + 8x = 10$
Find $\frac{1}{2}$ of $b$ and add the square of that number $(\frac{b}{2})^2$ to both sides of the equation	Think $b = 8$ $\frac{1}{2}b = 4 \text{ and } 4^2 = 16$ $x^2 + 8x = 10$ $x^2 + 8x + 16 = 10 + 16$
The left side is now a perfect square trinomial (PST), so factor it.	$(x + 4)(x + 4) = 26$ $(x + 4)^2 = 26$
Find the square root of each side.	$(x + 4)^2 = 26$ $x + 4 = \pm\sqrt{26}$
Solve for $x$	$x = -4 \pm \sqrt{26}$

**Solve each quadratic by completing the square.**

1)  $a^2 + 2a - 3 = 0$

7)  $m^2 - 12m + 26 = 0$

2)  $a^2 - 2a - 8 = 0$

8)  $x^2 + 12x + 20 = 0$

3)  $p^2 + 16p - 22 = 0$

9)  $k^2 - 8k - 48 = 0$

4)  $k^2 + 8k + 12 = 0$

10)  $p^2 + 2p - 63 = 0$

5)  $r^2 + 2r - 33 = 0$

11)  $m^2 + 2m - 48 = -6$

6)  $a^2 - 2a - 48 = 0$

12)  $p^2 - 8p + 21 = 6$